

Algebra I Diocese of Greensburg Curriculum

Unit Standards Content Skills

Introduction to Algebra

CCSS: Mathematics
CCSS: HS: Algebra

Seeing Structure in Expressions HSA-SSE.A. Interpret the structure of expressions.

HSA-SSE.A.1. Interpret expressions that represent a quantity in terms of its context.

HSA-SSE.A.1a. Interpret parts of an expression, such as terms, factors, and coefficients.

HSA-SSE.A.2. Use the structure of an expression to identify ways to rewrite it.

HSA-SSE.B. Write expressions in equivalent forms to solve problems.

HSA-SSE.B.3. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.

Mathematical Practice

MP.The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students.

MP.1. Make sense of problems and persevere in solving them.

MP.2. Reason abstractly and quantitatively.

Absolute Values

- Inverse Operations
- Order of Operations
- Operations with Integers
- Prime Number
- Words to Expressions with Variables

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Knowledge

- Match equations and expressions to their written descriptions.
- Define a coefficient, composite number and constant.
- Define the Additive and Multiplicative Inverse.
- Identify and recall prime numbers.

Comprehension

- Locate points on a coordinate plane.
- Use the Estimation Strategy to predict a solution.
- Utilize Inverse Operations to solve an equation.
- Add/subtract/multiply/divide integers.

Application

- Relate equations to real world issues.
- Calculate the absolute value.
- Use Order of Operations to simplify an expression.

Analysis

Construct equations based on a written prompt.

Synthesis

Unit	Standards	Content	Skills
	MP.3. Construct viable arguments and critique the reasoning of others.		 Formulate Expressions and Equations from written words
	MP.4. Model with mathematics.		
	MP.5. Use appropriate tools strategically.		
	MP.6. Attend to precision.		
	MP.7. Look for and make use of structure.		
	MP.8. Look for and express regularity in repeated reasoning.		
	NCTM: Mathematics		
	NCTM: Grades 9 - 12		
	Algebra Understand patterns, relations, and functions		
	understand and perform transformations such as arithmetically combining, composing, and inverting commonly used functions, using technology to perform such operations on more-complicated symbolic expressions		
	Represent and analyze mathematical situations and structures using algebraic symbols		
	understand the meaning of equivalent forms of expressions, equations, inequalities, and relations;		

Use mathematical models to represent and understand quantitative relationships

use symbolic expressions, including iterative and recursive forms, to represent relationships arising from various contexts;

Data Analysis & Probability

Formulate questions that can be addressed with data and collect, organize, and display relevant data to answer them

understand the meaning of measurement data and categorical data, of univariate and bivariate data, and of the term variable

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Solving Equations

CCSS: Mathematics CCSS: HS: Algebra

Creating Equations

HSA-CED.A. Create equations that describe numbers or relationships.

HSA-CED.A.1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

HSA-CED.A.2. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

- Properties of Equality
 - Consecutive Integers
 - Associative Property
 - Commutative Property
 - Distributive Property
 - Reflexive Property
 - Symmetric Property
 - Transitive Property
- One-Step Equations
- Two-Step Equations
- Multi-Step Equations
- Equations with Variables on both Sides

Knowledge

- Point out the different transformations being applied in an equation.
- Identify the Properties of Equality
- Identify what properties are being used to solve equations.
- Recognize properties of equations.

Comprehension

- Explain the process for solving equations.
- Set and Solve a proportion.

Application

Solve multi-step equations

Unit **Skills Standards** Content HSA-CED.A.4. Rearrange formulas to Arithmetic Sequence Apply properties of equations. highlight a quantity of interest, using the **Inverse Operation** same reasoning as in solving equations. **Solving Proportions Analysis** Translating and Solving **Literal Equations** Understand and Interpret the use **Reasoning with Equations & Inequalities** of ratios and proportions to **HSA-REI.A.** Understand solving compare and represent equations as a process of reasoning quantitative relationships. and explain the reasoning. **Synthesis** HSA-REI.A.1. Explain each step in solving a simple equation as following from the equality of numbers asserted at the Synthesize information to set up a proportion and solve. previous step, starting from the assumption Translating and solving literal that the original equation has a solution. Construct a viable argument to justify a equations. solution method. Transform equations using the four operations. **HSA-REI.B.** Solve equations and Write equations to represent inequalities in one variable. relationships among integers. HSA-REI.B.3. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. **NCTM: Mathematics** NCTM: Grades 6 - 8 **Number & Operations** Understand numbers, ways of representing numbers, relationships among numbers, and number systems work flexibly with fractions, decimals, and percents to solve problems; develop meaning for integers and represent and compare quantities with them. **Understand meanings of operations** and how they relate to one another

understand the meaning and effects of arithmetic operations with fractions, decimals, and integers;

use the associative and commutative properties of addition and multiplication and the distributive property of multiplication over addition to simplify computations with integers, fractions, and decimals;

understand and use the inverse relationships of addition and subtraction, multiplication and division, and squaring and finding square roots to simplify computations and solve problems.

Compute fluently and make reasonable estimates

develop and analyze algorithms for computing with fractions, decimals, and integers and develop fluency in their use;

Algebra

Represent and analyze mathematical situations and structures using algebraic symbols

use symbolic algebra to represent situations and to solve problems, especially those that involve linear relationships;

recognize and generate equivalent forms for simple algebraic expressions and solve linear equations

Use mathematical models to represent and understand quantitative relationships

model and solve contextualized problems using various representations, such as graphs, tables, and equations.

Unit	Standards	Content	Skills
	Measurement Apply appropriate techniques, tools, and formulas to determine measurements solve simple problems involving rates and derived measurements for such attributes as velocity and density. © Copyright 2010. National Governors Association Center for Best Practices and Council of Chief State School Officers. All rights reserved.		
Inequalities	CCSS: HS: Algebra Creating Equations HSA-CED.A. Create equations that describe numbers or relationships. HSA-CED.A.1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. HSA-CED.A.2. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. Reasoning with Equations & Inequalities HSA-REI.A. Understand solving equations as a process of reasoning and explain the reasoning. HSA-REI.A.1. Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution.	 Problem Solving Strategies Inequalities with One Variable Solution Sets of Inequalities Absolute Value Inequalities with Two Variables Systems of Linear Inequalities 	 Comprehension Identify methods for solving inequalities Application Graph inequalities in one variable Graph inequalities with two variables Graph systems of inequalities. Graph solution sets for absolute value problems Apply knowledge to real world problems Explain the solution set of a system of inequalities Evaluation Relate systems of inequalities to real world problems.

Construct a viable argument to justify a solution method.

HSA-REI.A.2. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

HSA-REI.B. Solve equations and inequalities in one variable.

HSA-REI.B.3. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

HSA-REI.C. Solve systems of equations.

HSA-REI.C.5. Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.

HSA-REI.C.8. (+) Represent a system of linear equations as a single matrix equation in a vector variable.

HSA-REI.D. Represent and solve equations and inequalities graphically.

HSA-REI.D.10. Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).

NCTM: Mathematics NCTM: Grades 9 - 12

Algebra

Represent and analyze mathematical situations and structures using algebraic symbols

write equivalent forms of equations, inequalities, and systems of equations and solve them with fluency-mentally or with

Unit Standards Content Skills

paper and pencil in simple cases and using technology in all cases;

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Linear Equations

CCSS: Mathematics CCSS: HS: Algebra

Creating Equations

HSA-CED.A. Create equations that describe numbers or relationships.

HSA-CED.A.1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

NCTM: Mathematics NCTM: Grades 9 - 12

Algebra

Understand patterns, relations, and functions

understand relations and functions and select, convert flexibly among, and use various representations for them;

analyze functions of one variable by investigating rates of change, intercepts, zeros, asymptotes, and local and global behavior:

understand and perform transformations such as arithmetically combining, composing, and inverting commonly used functions, using technology to perform such operations on more-complicated symbolic expressions

- Slope of a line
- X and Y Intercepts
- Linear Equations and their Graphs
- Standard Form of Linear Equation
- Slope Intercept Form of a Linear Equation
- Point Slope Form of a Linear Equation
- Parallel and Perpendicular lines
- Function Rules, Tables, and Graphs
- Direct Variation
- Distance/Time
- Relating Graphs to Events

Knowledge

- Understand the difference between a relation and a function.
- Define Functions, Tables and Graphs
- Identify a linear function.
- Identify the x and y intercepts of a graph.

Comprehension

- Calculate direct variation.
- Calculate the x and y intercepts given an equation.

Application

- Graph a linear equation.
- Calculate the slope of a line given a graph.
- Calculate the perimeter and area as a function of length/width
- Calculate the slope of a line from two points

Analysis

 Develop the equation of a line using slope, x-intercept, and pointslope form.

Unit	Standards	Content	Skills
	understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions; interpret representations of functions of two variables		 Construct the equation of a line in standard form, slope intercept form, or point slope form. Distinguish whether a relation is a function given a table or graph.
	Represent and analyze mathematical situations and structures using algebraic symbols use a variety of symbolic representations, including recursive and parametric		 Develop and Linear Equation given data. (Best fit line) Match a graph to an event.
	equations, for functions and relations; Use mathematical models to represent and understand quantitative relationships		 Summarize data to solve Distance/Time problems
	identify essential quantitative relationships in a situation and determine the class or classes of functions that might model the relationships;		•
	use symbolic expressions, including iterative and recursive forms, to represent relationships arising from various contexts;		
	Geometry Apply transformations and use symmetry to analyze mathematical situations		
	understand and represent translations, reflections, rotations, and dilations of objects in the plane by using sketches, coordinates, vectors, function notation, and matrices;		
	Data Analysis & Probability Select and use appropriate statistical methods to analyze data		

HSA-CED.A.2. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

Reasoning with Equations & Inequalities **HSA-REI.B.** Solve equations and inequalities in one variable.

HSA-REI.B.3. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

HSA-REI.C. Solve systems of equations.

- Strategies
- Scatter Plots
- Solve and Graph Absolute Value Equations

Application

- Solve absolute value equations
- Graph absolute value equations
- Graph a system of equations
- Identify solutions set of a system of equations

Analysis

Explain when a system of equations will have no solution or infinite solutions.

Unit Standards Content Skills

HSA-REI.C.6. Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.

HSA-REI.D. Represent and solve equations and inequalities graphically.

HSA-REI.D.10. Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).

NCTM: Mathematics NCTM: Grades 9 - 12

Algebra

Understand patterns, relations, and functions

generalize patterns using explicitly defined and recursively defined functions;

understand and perform transformations such as arithmetically combining, composing, and inverting commonly used functions, using technology to perform such operations on more-complicated symbolic expressions

interpret representations of functions of two variables

Use mathematical models to represent and understand quantitative relationships

draw reasonable conclusions about a situation being modeled.

Analyze change in various contexts

approximate and interpret rates of change from graphical and numerical data.

Synthesis

- Develop a Parallel or Perpendicular line given a point and an equation.
- Predict the line of best-fit, given a scatter plot.

Unit Standards Content Skills

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Mid Term Exam

Polynomials and Exponents

CCSS: Mathematics CCSS: HS: Algebra

Arithmetic with Polynomials & Rational Functions

HSA-APR.A. Perform arithmetic operations on polynomials.

HSA-APR.A.1. Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

HSA-APR.B. Understand the relationship between zeros and factors of polynomials.

HSA-APR.B.2. Know and apply the Remainder Theorem: For a polynomial p(x) and a number a, the remainder on division by x - a is p(a), so p(a) = 0 if and only if (x - a) is a factor of p(x).

HSA-APR.B.3. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

HSA-APR.C. Use polynomial identities to solve problems.

- Adding and Subtracting Polynomials
- Degree of Polynomial
- Integer Exponents
- Multiplying
 - Monomials
 - Monomial by a Polynomial
 - o Polynomials
 - Binomials
- Polynomial Function
- Problem solving strategies

Knowledge

- Identify the degree of a polynomial.
- Define an exponent.
- List components of expressions as like terms.

Comprehension

- Simplify expressions involving monomial-monomial and monomial-polynomial multiplication.
- Write and simplify expressions involving exponents.

Application

- Multiply monomials, binomials and polynomials.
- Use rules of exponents to solve equations.

Analysis

 Use different strategies to solve problems HSA-APR.C.4. Prove polynomial identities and use them to describe numerical relationships.

HSA-APR.D. Rewrite rational expressions.

HSA-APR.D.6. Rewrite simple rational expressions in different forms; write a(x)/b(x) in the form q(x) + r(x)/b(x), where a(x), b(x), q(x), and r(x) are polynomials with the degree of r(x) less than the degree of r(x), using inspection, long division, or, for the more complicated examples, a computer algebra system.

NCTM: Mathematics NCTM: Grades 9 - 12

Algebra

Understand patterns, relations, and functions

understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions;

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Factoring

CCSS: Mathematics CCSS: HS: Algebra

Seeing Structure in Expressions HSA-SSE.B. Write expressions in equivalent forms to solve problems.

Factoring

- Binomials
- Difference of Two Square
- Perfect Square Trinomials
- Trial and Error
- Trinomials
- Factoring by Grouping

Knowledge

List factors to solve a polynomial equations.

Comprehension

Unit **Skills Standards** Content **Greatest Common** HSA-SSE.B.3a. Factor a quadratic Factor Describe the process of "Factoring expression to reveal the zeros of the Prime Factorization by Grouping" and explain why it function it defines. Solving Equations by works. Factoring **Arithmetic with Polynomials & Rational** Zero Product Property **Functions**

Explore patterns for

Factoring

HSA-APR.B. Understand the relationship between zeros and factors of polynomials.

HSA-APR.B.2. Know and apply the Remainder Theorem: For a polynomial p(x)and a number a, the remainder on division by x - a is p(a), so p(a) = 0 if and only if (x - a)- a) is a factor of p(x).

HSA-APR.B.3. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

Reasoning with Equations & Inequalities **HSA-REI.B.** Solve equations and inequalities in one variable.

HSA-REI.B.4b. Solve quadratic equations by inspection (e.g., for $x^2 = 49$), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as a ± bi for real numbers a and b.

NCTM: Mathematics NCTM: Grades 9 - 12

Algebra

Represent and analyze mathematical situations and structures using algebraic symbols

use symbolic algebra to represent and explain mathematical relationships;

Application

- Apply the FOIL method to check answers.
- Factor expressions and equations.
- Solve an equation by factoring.

Analysis

- Identify the appropriate method to factor an expression or equation.
- Identify the GCF of polynomial expressions.
- Examine patterns for factoring

Pythagorean Theorem.

8.G.B.6. Explain a proof of the Pythagorean Theorem and its converse.

8.G.B.7. Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions.

CCSS: HS: Algebra

Reasoning with Equations & Inequalities HSA-REI.A. Understand solving equations as a process of reasoning and explain the reasoning.

HSA-REI.A.2. Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

NCTM: Mathematics

- Simplify Radicals Including Variables Assumed to be Positive
- Rational Numbers as **Decimals and Fractions**
- Pythagorean Theorem
- Radical Equations

Identify repeating decimals

Comprehension

- Simplify expressions involving radicals including variables assumed to be positive.
- Multiply and Divide Radicals
- Add and Subtract Radicals

Analysis

Simplify and rationalize radicals

Application

Solve variable equations involving radicals, including rational and irrational solutions.

Unit	Standards	Content	Skills
	NCTM: Grades 9 - 12 Algebra Understand patterns, relations, and functions		 Use the Pythagorean theorem to solve problems
	understand relations and functions and select, convert flexibly among, and use various representations for them;		
	Represent and analyze mathematical situations and structures using algebraic symbols		
	understand the meaning of equivalent forms of expressions, equations, inequalities, and relations;		
	judge the meaning, utility, and reasonableness of the results of symbol manipulations, including those carried out by technology.		
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Quadratic Equations	CCSS: Mathematics CCSS: HS: Algebra Creating Equations HSA-CED.A. Create equations that describe numbers or relationships. HSA-CED.A.1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.	 Quadratic Formula Quadratic Equations with Perfect Squares Methods of Solving Quadratic Equations Graphs of Quadratic Equations 	 Identify quadratic formula Identify components of a quadratic graph Identify perfect squares Explain why the quadratic formula can be used to solve all quadratic equations Comprehension
	Reasoning with Equations & Inequalities HSA-REI.B. Solve equations and inequalities in one variable.		 Understand which method to use to solve a quadratic equation

Unit	Standards	Content	Skills
	HSA-REI.B.4. Solve quadratic equations in one variable. HSA-REI.B.4b. Solve quadratic equations by inspection (e.g., for x² = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as a ± bi for real numbers a and b. © Copyright 2010. National Governors Association Center for Best Practices and Council of Chief State School Officers. All rights reserved.		 Application Apply the quadratic formula to solve equations Identify solutions set of a quadratic equation Analysis Select the best method for solving a quadratic equation Analyze a quadratic function
Rational Expressions (Algebraic Fractions)	CCSS: HS: Algebra Arithmetic with Polynomials & Rational Functions HSA-APR.D. Rewrite rational expressions. HSA-APR.D.7. (+) Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions. NCTM: Mathematics NCTM: Grades 9 - 12 Algebra Understand patterns, relations, and functions understand and compare the properties of classes of functions, including exponential,	 Adding and Subtracting Rational Expressions Multiplying and Dividing Rational Expressions Polynomial Long Division Simplifying Rational Expressions 	 Knowledge Recognize the possible values of a variable in the denominator of a variable expression. Use Polynomial Long Division to calculate a quotient. Comprehension Simplify rational expressions. Application Use knowledge of a LCD to add or subtract rational expressions. Use knowledge of factoring to multiply and divide rational expressions Analysis

Unit	Standards	Content	Skills	
	polynomial, rational, logarithmic, and periodic functions; © Copyright 2010. National Governors Association Center for Best Practices and Council of Chief State School Officers. All rights reserved.		 Defend whether rational expressions have been correctly simplified, using their knowledge of fraction manipulation. 	
Statistics & Probability	CCSS: Mathematics CCSS: HS: Stats/Prob	 Display of Data Bar Graph Box & Whisker Plot Circle Graph (Pie Graph) 	Knowledge	
	Interpreting Categorical & Quantitative Data HSS-ID.A. Summarize, represent, and interpret data on a single count or		 Interpret various statistical graphs. (Bar, Box & Whisker, Stem & Leaf, Pie chart) 	
	measurement variable	Stem & LeafPlot	Application	
	HSS-ID.A.1. Represent data with plots on the real number line (dot plots, histograms, and box plots).	 Concepts of Probability: Odds Simple Event Independent 	 Calculate the Measure of Central Tendency (Mean, Median and Mode) 	
	HSS-ID.A.2. Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard	Events o Dependent Events o Independent	 Calculate the probability of event. Given the domain calculate the range and interquartile range. 	
	deviation) of two or more different data sets.	Variable ⊙ Dependent	Analysis	
	NCTM: Mathematics NCTM: Grades 9 - 12	Variable ○ Compound Event	 Calculate and/or make predication based upon measures of central tendency 	
	Data Analysis & Probability Formulate questions that can be addressed with data and collect,	 Concepts of Statistics Domain Range Measure of 	 Apply probability to practical situations, including compound even. 	
	organize, and display relevant data to answer them	Central Tendency	Synthesis	
	understand histograms, parallel box plots,	Line of Best Fit	Recognize and evaluate random	

Quartile

Outlier

Interquartile

and scatterplots and use them to display

compute basic statistics and understand the distinction between a statistic and a

data;

parameter.

 Recognize and evaluate random processes underlying statistical experiments understand how sample statistics reflect the values of population parameters and use sampling distributions as the basis for informal inference;

evaluate published reports that are based on data by examining the design of the study, the appropriateness of the data analysis, and the validity of conclusions;

understand how basic statistical techniques are used to monitor process characteristics in the workplace.

Understand and apply basic concepts of probability

understand the concepts of sample space and probability distribution and construct sample spaces and distributions in simple cases;

use simulations to construct empirical probability distributions;

compute and interpret the expected value of random variables in simple cases;

understand the concepts of conditional probability and independent events;

understand how to compute the probability of a compound event.

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Unit	Standards	Content	Skills
Final Term Exam			

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