Algebra II
Diocese of Greensburg Curriculum


HSF-IF.A.3. Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers.

## HSF-IF.C. Analyze functions using different representations.

HSF-IF.C.7b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.

## Building Functions

HSF-BF.A. Build a function that models a relationship between two quantities.

HSF-BF.A.2. Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.

## HSF-BF.B. Build new functions from existing functions.

HSF-BF.B.3. Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

## CCSS: HS: Geometry

Expressing Geometric Properties with Equations
HSG-GPE.B. Use coordinates to prove simple geometric theorems algebraically

HSG-GPE.B.5. Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).

## NCTM: Grades 9-12

## Number \& Operations <br> Compute fluently and make reasonable estimates

judge the reasonableness of numerical computations and their results.

## Algebra

Understand patterns, relations, and functions
generalize patterns using explicitly defined and recursively defined functions;
understand relations and functions and select, convert flexibly among, and use various representations for them
analyze functions of one variable by investigating rates of change, intercepts, zeros, asymptotes, and local and global behavior;

Represent and analyze mathematical situations and structures using algebraic symbols
understand the meaning of equivalent forms of expressions, equations, inequalities, and relations;
write equivalent forms of equations, inequalities, and systems of equations and solve them with fluencymentally or with paper and pencil in simple cases and using technology in all cases;
use symbolic algebra to represent and explain mathematical relationships;

## Analyze change in various contexts

approximate and interpret rates of change from graphical and numerical data.

## Data Analysis \& Probability <br> Select and use appropriate statistical methods to analyze data

recognize how linear transformations of univariate data affect shape, center, and spread;

| Unit | Standards | Content | Skills |
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| Linear Systems | CCSS: Mathematics CCSS: HS: Algebra | - Methods to Solve Systems of Equations <br> - Elimination <br> - Substitution <br> - Graph Systems of Linear Inequalities <br> - Solve Systems of Linear Inequalities <br> - Solve 3-Variable Systems of Equations using Elimination and Substituion | The students will be able to: <br> Comprehension <br> - Understand systems of equations <br> - Convert word problems into a system of equations <br> Application |
|  | Reasoning with Equations \& Inequalities HSA-REI.C. Solve systems of equations. |  |  |
|  | HSA-REI.C.6. Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables. |  |  |
|  | HSA-REI.D. Represent and solve equations and inequalities graphically. |  |  |
|  | HSA-REI.D.12. Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. |  | - Graph systems of linear inequalities <br> - Solve systems of linear inequalities |
|  | NCTM: Mathematics <br> NCTM: Grades 9-12 |  | Analysis |
|  | Algebra <br> Represent and analyze mathematical situations and structures using algebraic symbols |  | - Identify which strategy to use on problems involving systems of equations |
|  | write equivalent forms of equations, inequalities, and systems of equations and solve them with fluencymentally or with paper and pencil in simple cases and using technology in all cases; |  |  |
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| Unit | Standards | Content | Skills |
| :---: | :---: | :---: | :---: |
| Quadratic Functions and Equations | CCSS: Mathematics <br> CCSS: HS: Num/Quantity <br> The Complex Number System <br> HSN-CN.C. Use complex numbers in polynomial <br> identities and equations. <br> HSN-CN.C.7. Solve quadratic equations with real coefficients that have complex solutions. <br> CCSS: HS: Algebra <br> Arithmetic with Polynomials \& Rational Functions HSA-APR.C. Use polynomial identities to solve problems. <br> HSA-APR.C.5. (+) Know and apply the Binomial Theorem for the expansion of $(x+y) n$ in powers of $x$ and $y$ for a positive integer $n$, where $x$ and $y$ are any numbers, with coefficients determined for example by Pascal's Triangle. <br> Reasoning with Equations \& Inequalities <br> HSA-REI.B. Solve equations and inequalities in one variable. <br> HSA-REI.B.4. Solve quadratic equations in one variable. <br> HSA-REI.B.4a. Use the method of completing the square to transform any quadratic equation in $x$ into an equation of the form $(x-p)^{2}=q$ that has the same solutions. Derive the quadratic formula from this form. HSA-REI.B.4b. Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. <br> Recognize when the quadratic formula gives complex solutions and write them as a $\pm$ bi for real numbers a and $b$. <br> CCSS: HS: Functions <br> Interpreting Functions <br> HSF-IF.C. Analyze functions using different representations. <br> HSF-IF.C.7a. Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> HSF-IF.C.8a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. <br> Building Functions <br> HSF-BF.B. Build new functions from existing functions. | Factoring <br> - Laws of Exponents <br> - Add, subtract, multiply polynomials <br> - Factoring GCF <br> - Factoring when a is not 1 <br> - Inverse FOIL <br> - Perfect Square Trinomial <br> - Difference of Two Squares <br> - Grouping <br> - Sum and Difference of Cubes <br> - Quadratic Formula <br> - Graphing in Standard, Vertex, and Intercept Form <br> - Complete the Square <br> - Inequalities <br> - Systems of Inequalities | The students will be able to: <br> Knowledge <br> - Know standard, vertex, and intercept form of a quadratic function <br> Comprehension <br> - Understand the difference when $\mathrm{a}=1$ and a is not 1 in $a x^{\wedge} 2+b x+c$ <br> Application <br> - Factor using trial and error, completing the square, and the quadratic formula <br> Analysis <br> - Factor recognizing a perfect square trinomial, difference of two squares <br> - Factor using sum and difference of cubes/grouping <br> Synthesis <br> - Create the quadratic formula by completing the square |

HSF-BF.B.3. Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
NCTM: Mathematics
NCTM: Grades 9-12
Number \& Operations
Understand numbers, ways of representing numbers, relationships among numbers, and number systems compare and contrast the properties of numbers and number systems, including the rational and real numbers, and understand complex numbers as solutions to quadratic equations that do not have real solutions;
Algebra
Understand patterns, relations, and functions understand and perform transformations such as arithmetically combining, composing, and inverting commonly used functions, using technology to perform such operations on more-complicated symbolic expressions understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions;
interpret representations of functions of two variables © Copyright 2010. National Governors Association Center for Best Practices and Council of Chief State School Officers. All rights reserved.

## Polynomials and Polynomial Functions

CCSS: Mathematics
CCSS: HS: Num/Quantity
The Complex Number System
HSN-CN.C. Use complex numbers in polynomial dentities and equations.
HSN-CN.C.8. (+) Extend polynomial identities to the complex numbers. For example, rewrite $x^{2}+4$ as ( $x+$ 2i) $(x-2 i)$.

- Polynomial Inequalities
- Graphing
- End Behavior
- Maximum and Minimum Points
- Zeros
- Fundamental Theorem of Algebra
- Find patterns in the functions for transformations


## The students will be able to:

## Knowledge

- State the Fundamental Theorem of Algebra

HSN-CN.C.9. (+) Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.
CCSS: HS: Algebra
Arithmetic with Polynomials \& Rational Functions HSA-APR.B. Understand the relationship between zeros and factors of polynomials
HSA-APR.B.2. Know and apply the Remainder
Theorem: For a polynomial $p(x)$ and a number $a$, the remainder on division by $x-a$ is $p(a)$, so $p(a)=0$ if and only if $(x-a)$ is a factor of $p(x)$.
HSA-APR.B.3. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
CCSS: HS: Functions
Interpreting Functions
HSF-IF.C. Analyze functions using different
representations.
HSF-IF.C.7c. Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior.
Building Functions
HSF-BF.B. Build new functions from existing functions.
HSF-BF.B.3. Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
NCTM: Mathematics
NCTM: Grades 9-12
Algebra
Understand patterns, relations, and functions understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions;
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- Calculate the Zeros of a Polynomial.
- Solve Polynomial Inequalities


## Application

- Use The Fundamental Theorem of Algebra to determine the roots of a polynomial.
- Sum and difference of cubes, grouping


## Analysis

- Determine the end behavior of a polynomial function
- Determine the maximum and minimum values of a polynomial.
- Graph polynomial functions.
- Graph polynomial inequalities.


## Mid Term Exam

Radical Functions
and Rational
Exponents

CCSS: Mathematics
CCSS: HS: Num/Quantity
The Real Number System
HSN-RN.A. Extend the properties of exponents to rational exponents.
HSN-RN.A.1. Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents.
Show details
HSN-RN.A.2. Rewrite expressions involving radicals and rational exponents using the properties of exponents.
The Complex Number System
HSN-CN.A. Perform arithmetic operations with complex numbers.
HSN-CN.A.1. Know there is a complex number $i$ such
that $\mathrm{i}^{2}=-1$, and every complex number has the form a

+ bi with a and b real.
HSN-CN.A.2. Use the relation $\mathrm{i}^{2}=-1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.
HSN-CN.A.3. (+) Find the conjugate of a complex
number; use conjugates to find moduli and quotients of complex numbers
HSN-CN.C. Use complex numbers in polynomial identities and equations.
HSN-CN.C.7. Solve quadratic equations with real
coefficients that have complex solutions.
CCSS: HS: Algebra
Reasoning with Equations \& Inequalities
HSA-REI.A. Understand solving equations as a process of reasoning and explain the reasoning.
HSA-REI.A.2. Solve simple rational and radical
equations in one variable, and give examples showing how extraneous solutions may arise.
CCSS: HS: Functions
Interpreting Functions
- nth Roots
- Properties of Exponents
- Properties of Radicals
- Simplify Radicals
- Graph Square and Cube Roots
- Rational Numbers
- Higher Order Radicals
- Algebraic Equations with Radicals
- Complex Numbers and Operations

The students will be able:

## Knowledge

- Know properties of exponents and radicals


## Comprehension

- Simplify radicals


## Application

- Simplify radical expressions
- Solve radical equations
- Simplify expressions involving complex numbers


## Analysis

- Transform graphs of square and cube roots

HSF-IF.C. Analyze functions using different representations.
HSF-IF.C.7b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
Building Functions
HSF-BF.A. Build a function that models a relationship
between two quantities
HSF-BF.A.1c. (+) Compose functions.
Show details
HSF-BF.B. Build new functions from existing functions
HSF-BF.B.3. Identify the effect on the graph of
replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
NCTM: Mathematics
NCTM: Grades 9-12
Number \& Operations
Understand numbers, ways of representing numbers, relationships among numbers, and number systems compare and contrast the properties of numbers and number systems, including the rational and real numbers, and understand complex numbers as solutions to quadratic equations that do not have real solutions;
Algebra
Understand patterns, relations, and functions understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions;
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| Exponential and | CCSS: Mathematics |
| :--- | :--- |
| Logarithmic | CCSS: HS: Algebra |
| Functions | Seeing Structure in Expressions |

Exponential Expressions

- Logarithmic Expressions
- Properties of Logarithmic Expressions

The students will be able:
Knowledge

HSA-SSE.B. Write expressions in equivalent forms to solve problems.
HSA-SSE.B.3c. Use the properties of exponents to transform expressions for exponential functions.
Show details
Reasoning with Equations \& Inequalities
HSA-REI.D. Represent and solve equations and inequalities graphically.
HSA-REI.D.11. Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y$ $=g(x)$ intersect are the solutions of the equation $f(x)=$
$g(x)$; find the solutions approximately, e.g., using
technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions
CCSS: HS: Functions
Interpreting Functions
HSF-IF.C. Analyze functions using different
representations.
HSF-IF.C.7e. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.
Linear, Quadratic, and Exponential Models
HSF-LE.A. Construct and compare linear and
exponential models and solve problems.
HSF-LE.A.1a. Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals. HSF-LE.A.3. Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.
NCTM: Mathematics
NCTM: Grades 9-12
Algebra
Understand patterns, relations, and functions understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions;

- Solving Exponential and Logarithmic Equations
- Graph Exponential and Logarithmic Equations
- Know how logarithms and exponentials are related
- Know properties of logarithmic and exponential expressions


## Comprehension

- Convert logarithmic expressions to exponential expressions and vice versa
- Combine logarithms via the laws of logarithms
- Graph exponential and logarithmic equations


## Application

- Solve exponential and logarithmic expressions
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## CCSS: Mathematics

CCSS: HS: Stats/Prob
Making Inferences \& Justifying Conclusions
HSS-IC.B. Make inferences and justify conclusions from sample surveys, experiments and observationa studies
HSS-IC.B.3. Recognize the purposes of and differences among sample surveys, experiments and observational studies; explain how randomization relates to each.
Conditional Probability \& the Rules of Probability
HSS-CP.B. Use the rules of probability to compute
probabilities of compound events in a uniform
probability model
HSS-CP.B.9. (+) Use permutations and combinations
to compute probabilities of compound events and solve problems.
NCTM: Mathematics
NCTM: Grades 9-12
Number \& Operations
Understand meanings of operations and how they
relate to one another
develop an understanding of permutations and
combinations as counting techniques.
Data Analysis \& Probability
Formulate questions that can be addressed with data and collect, organize, and display relevant data to answer them
compute basic statistics and understand the distinction between a statistic and a parameter.
Select and use appropriate statistical methods to analyze data
for univariate measurement data, be able to display the distribution, describe its shape, and select and calculate summary statistics;
Develop and evaluate inferences and predictions that are based on data

- Fundamental counting principle
- Permutations
- Combinations
- Experimental probability
- Theoretical probability
- Independent/dependent events
- Probability of multiple events
- Frequency table
- Conditional probability
- Analyzing data
- Measures of central tendencies
- Standard deviation
- Variance
- Binomial distribution
- Normal Distributions


## The students will be able: Knowledge

- Explain the differences between permutations and combinations.
- Know the Fundamental counting principle.
- Know the difference between experimental and theoretical probability,


## Comprehension

- List data in charts or graphs
- Construct a frequency table.
- Calculate the measures of central tendency
- Calculate the standard deviation


## Application

- Calculate the Probability of events occurring.
- Determine the binomial and normal distributions
use simulations to explore the variability of sample statistics from a known population and to construct sampling distributions;
understand how sample statistics reflect the values of population parameters and use sampling distributions as the basis for informal inference;
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## Rational

 Functions
## CCSS: Mathematics

## CCSS: HS: Algebra

## Arithmetic with Polynomials \& Rational Functions

 HSA-APR.A. Perform arithmetic operations on polynomials.HSA-APR.A.1. Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

## HSA-APR.B. Understand the relationship <br> between zeros and factors of polynomials.

HSA-APR.B.3. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

- Rational Algebraic Expressions
- Sums and Differences of Rational Functions
- Products and Quotients of Rational Functions
- Graphing Rational Functions
- Solve Rational Equations

The students will be able:

## Knowledge

- Simplify rationa expressions


## Comprehension

- Add and Subtract Rational Functions
- Multiply and Divide Rational Functions


## Application

- Solve Rational Equations.

HSA-APR.D. Rewrite rational expressions.

HSA-APR.D.6. Rewrite simple rational expressions in different forms; write $a(x) / b(x)$ in the form $q(x)+$ $r(x) / b(x)$, where $a(x), b(x), q(x)$, and $r(x)$ are polynomials with the degree of $r(x)$ less than the degree of $b(x)$, using inspection, long division, or, for the more complicated examples, a computer algebra system.

## Creating Equations HSA-CED.A. Create equations that describe numbers or relationships.

HSA-CED.A.1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

## CCSS: HS: Functions

## Interpreting Functions <br> HSF-IF.C. Analyze functions using different representations

HSF-IF.C.7d. (+) Graph rational functions, identifying zeros and asymptotes when suitable factorizations are available, and showing end behavior.

## Building Functions

HSF-BF.B. Build new functions from existing functions.

HSF-BF.B.3. Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

## NCTM: Mathematics

NCTM: Grades 9-12

## Algebra

Understand patterns, relations, and functions

- Find the Asymptotes of rational functions


## Analysis

- Graph Rational Equations
understand and compare the properties of classes of functions, including exponential, polynomial, rational, logarithmic, and periodic functions;
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## Quadratic <br> Relations and <br> Conic Sections

## CCSS: Mathematics

CCSS: HS: Algebra

## Seeing Structure in Expressions

HSA-SSE.B. Write expressions in equivalent forms to solve problems.

HSA-SSE.B.3a. Factor a quadratic expression to reveal the zeros of the function it defines.

HSA-SSE.B.3b. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.

## Reasoning with Equations \& Inequalities

 HSA-REI.C. Solve systems of equations.HSA-REI.C.7. Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. For example, find the points of intersection between the line $y=-$ $3 x$ and the circle $x^{2}+y^{2}=3$.

## CCSS: HS: Geometry

Expressing Geometric Properties with Equations HSG-GPE.A. Translate between the geometric description and the equation for a conic section

HSG-GPE.A.1. Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

HSG-GPE.A.2. Derive the equation of a parabola given a focus and directrix.

- Circles with Center and Radius
- Parabolas with Directrix and Focus
- Ellipses with Foci, Major and Minor Axes, and Translations
- Hyperbolas with Foci, Graphing Box, and Asymptotes

| Unit | Standards | Content | Skills |
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|  | HSG-GPE.A.3. (+) Derive the equations of ellipses and hyperbolas given two foci for the ellipse, and two directrices of a hyperbola. <br> © Copyright 2010. National Governors Association Center for Best Practices and Council of Chief State School Officers. All rights reserved. |  |  |
| Introduction to Trigonometry* | CCSS: Mathematics CCSS: HS: Geometry | - Ratios of Trig Functions <br> - Right Triangle Problems | The students will be able: Comprehension |
|  | Similarity, Right Triangles, \& Trigonometry HSG-SRT.C. Define trigonometric ratios and solve problems involving right triangles | - Properties of Special Right Triangles <br> - Radian Measure | - Understand the relation between degrees and radians |
|  | HSG-SRT.C.6. Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. |  | Application <br> - Apply ratio of trig |
|  | HSG-SRT.C.7. Explain and use the relationship between the sine and cosine of complementary angles. |  | functions to discover a missing side of a right triangle <br> - Find missing sides of |
|  | HSG-SRT.C.8. Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems. |  | special right triangles |
|  | NCTM: Mathematics <br> NCTM: Grades 9-12 |  |  |
|  | Geometry <br> Analyze characteristics and properties of twoand three-dimensional geometric shapes and develop mathematical arguments about geometric relationships |  |  |
|  | use trigonometric relationships to determine lengths and angle measures. |  |  |
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